Radar Signal Classification System Based on BP Neural Network

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Abstract: This paper introduces a method of recognition and classification of radar echo signals. We introduce the method of radar signal preprocessing, including the construction of complex echo signals of radar and the normalization of spectrums. Besides, we calculate the power spectral density (PSD) and extract the features. Then we construct the back propagation (BP) neural network as the classifier. Finally, we conduct the simulation experiment and analyze the experimental results. From the experimental results, it can be seen that this method is better than the traditional single-layer neural network recognition method. In addition, our method can not only maintain a better classification accuracy of radar signals despite the low signal-to-noise ratio, but also reduce the classification gap between different radar signals, with good stability and robustness.

Keywords: Power Spectral Density, Back Propagation Neural Network, Feature Extraction

1. Introduction

With the development of science and technology, radar can not only benefit human beings in daily life, but also play an indispensable role in modern warfare [1]. If the radar signals can be identified accurately and efficiently, it will have a profound impact on the research in the fields of missile warning, atmospheric detection, and target tracking [2]. Therefore, this paper addresses the problem of radar signal identification and classification.

A lot of research has been done on the topic of "identification and classification of radar signals in complex environments". Li YJ [3] introduced an integral rotation factor, and used a radial integration method creatively. However, this method is sensitive to noise, and the recognition accuracy is low at low signal-to-noise ratio. HU H [4] applied spectral correlation analysis and used Gaussian kernel-support vector machine as a classifier for radar signal recognition, which has better robustness and robustness. Dudul [5] used neural networks to classify radar echo signals in ionospheric studies with novel research ideas. However, the method is not generalizable and less resistant to interference. Iglesias [6] used an automatic modulation classifier with low complexity signal features and hierarchical decision trees, which has the advantage of efficiency and immediacy. WANG Y C [7] used Morlet method, which uses wavelet ridges after signal wavelet transform as features for radar signal classification. However, this method is computationally intensive and has low recognition efficiency. WANG Q [8] linked convolutional neural network with bidirectional long and short-term memory network and obtained higher recognition success rate. However, if the radar signal type is added, the classification accuracy decreases significantly.

In summary, the existing methods can achieve good results for signal classification, but there are still problems of poor interference immunity and low classification accuracy under low signal-to-noise ratio conditions.

In order to improve the accuracy of radar signal identification and classification, combining the valuable experience of previous authors, this paper proposes a radar signal classification method. First, constructing the complex echo signals and implementing the normalization process on the spectrum of the echo signal. Second, calculating the PSD of different echo signals, taking the sub-band power ratio as the feature parameter. Finally, the BP neural network is used for classification. The classification results of this paper were compared and analyzed with the traditional single-layer neural network recognition method. All in all, this method has higher recognition accuracy and stronger anti-interference ability.

2. Feature extraction based on PSD of radar signals

Common signal feature extraction methods include: extraction of signal over zero rate; calculation of signal short-time energy and short-time autocorrelation function; calculation of frequency standard deviation; extraction of resonance peaks, etc. In this paper, the PSD of the radar echo signal is characterized by feature extraction, which has low execution complexity, significant signal characterization, and strong resistance to environmental interference.

2.1 Constructing demodulated echo signals

To the beginning, in practice, the radar transmits a real signal, but the signal is artificially demodulated in two ways to construct a complex echo signal [9]. In the conventional method, the radar will mix the received signal to obtain a demodulated echo signal consisting of two echoes of I, Q.

The linear frequency modulated signal (LMF) is one of the pulse compression techniques, which is very important in practical applications and can effectively solve the contradiction between the distance of action and the distance resolution of the radar system. The LMF signal is easy to generate and process, and is technically mature. Besides, its instantaneous frequency is a linear function of time, and a uniform signal bandwidth can be obtained, which has been widely used.

Taking the classical LMF signal as an example, its radar emission signal can be expressed as

$$x_{LFM}(t) = \cos[2\pi f_0 t + k\pi t^2]\left[u(t) - u(t - \tau_p)\right] \tag{1}$$

The carrier signal of I channel is $\cos(2\pi f_0 t)$, the carrier signal of Q channel is $\cos(2\pi f_0 t + \frac{\pi}{2})$, and the constructed complex demodulated echo signal is $y_I(t)$ and $y_Q(t)$.

$$
\begin{aligned}
y_I(t) &= \sigma \cos[2\pi f_0(t - t_0) + k\pi(t - t_0)^2]\cos(2\pi f_0 t) \\
&= \sigma \frac{\cos[-2\pi f_0 t_0 + k\pi(t - t_0)^2] + \cos(4\pi f_0 t - 2\pi f_0 t_0 + k\pi(t - t_0)^2)}{2}
\end{aligned} \tag{2}
$$

$$
\begin{aligned}
y_Q(t) &= \sigma \cos[2\pi f_0(t - t_0) + k\pi(t - t_0)^2]\cos(2\pi f_0 t + \frac{\pi}{2}) \\
&= \sigma \frac{\sin[-2\pi f_0 t_0 + k\pi(t - t_0)^2] + \sin(4\pi f_0 t - 2\pi f_0 t_0 + k\pi(t - t_0)^2)}{2}
\end{aligned} \tag{3}
$$

As the second term in the expression of the two-way echo signal is much higher in frequency than the first term in practical applications, the second term can be filtered out by a low-pass filter, so the demodulated echo signal can be expressed as $y_s(t)$.

$$
\begin{aligned}
y_s(t) &= y_I(t) + jy_Q(t) \\
&= \frac{\sigma}{2}\{\cos[-2\pi f_0 t_0 + k\pi(t - t_0)^2] + j\sin[-2\pi f_0 t_0 + k\pi(t - t_0)^2]\} \\
&= \frac{\sigma}{2}e^{j[-2\pi f_0 t_0 + k\pi(t - t_0)^2]}
\end{aligned} \tag{4}
$$

2.2 Calculate the PSD of the echo signal

In the frequency domain of the discrete time Fourier transform (DTFT). Formally, the sequences at both ends of the transform (in the time and frequency domains) are finite-length, while in practice both sets of sequences should be considered as principal value sequences of discrete periodic signals. For a finite-length discrete signal to be DFT, it is usually considered as a periodic signal that has been periodically extended and then transformed.

After obtaining the radar echo signal, this paper uses DFT to calculate the PSD of the echo signal.

The basic formula of DFT is as follows:

$$
\begin{aligned}
y(n) &= y_s(t)|_{t=nT} \\
y(k) &= \sum_{n=0}^{N-1} y(n)e^{-j\frac{2\pi}{N}nk}
\end{aligned} \tag{5}
$$

T is the sampling period.

In our experiment, the DFT of the echo signal was done with N=2024. In order to facilitate the extraction of classification features, the DFT spectrum of the echo signal was normalized before obtained its PSD. Figure 1 shows the normalized PSD image of the classical LMF signal.
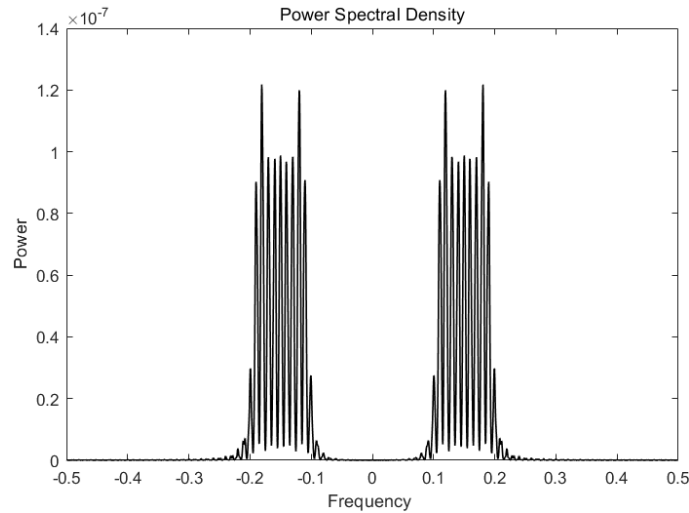

Figure 1: PSD image after normalization of classical LMF signal

In this paper, we took the positive semi-axis region of the normalized PSD image and divided it uniformly into five intervals. Each interval is called a sub-band, and the power ratio G_i of sub-band i was calculated as follows [10].

$$G_i = \frac{1}{P} \sum_{j=(i-1)*u}^{F_i} PSD_j \times f_r \times 100\% \ (i = 1,2,3,4,5)$$

$$P = \sum_{j=0}^{F_5} PSD_j \times f_r$$

(6)

F_i denotes the cutoff frequency of sub-band i, f_r is the frequency resolution, PSD_j is the power spectral density at frequency j, and P is the total power.

The power ratios of these five intervals are used as classification features for the BP neural network. In this paper, five common radar signals [11] were used, as followed: rectangular pulse signal (CP), linear frequency modulated pulse signal (LMF), binary phase shift keying pulse signal (BPSK), Frank multiphase coded signal (Frank) and Costas signal.

3. Construction of BP neural network classification system

The common classifiers for radar signals are neural networks, Gaussian kernel-support vector machines, random forests, etc. BP neural network, a classifier with strong nonlinear mapping and fault tolerance capabilities, has high adaptability to our data. As a result, we chose BP neural network as the classifier for this paper.
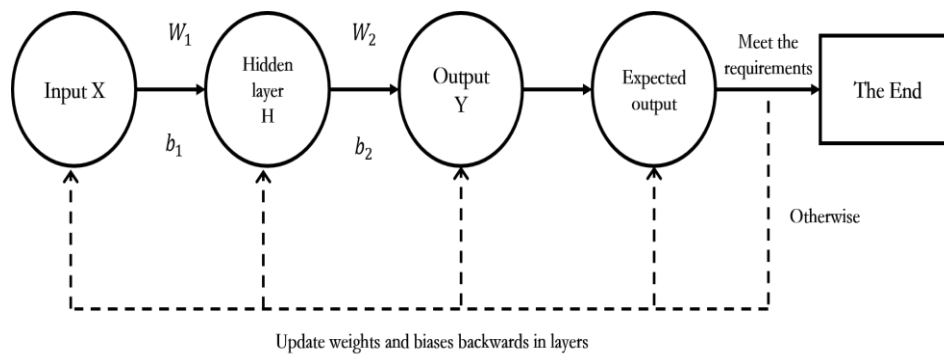

Figure 2: Schematic diagram of BP neural network

BP neural network is trained by computer simulation on the basis of raw data to obtain classification rules. It can get the closest result to the desired output value for the given input value. Its main feature is that the signal propagates forward through the weights w_i, while the error propagates backward through the feedback b_i. The schematic diagram of BP neural network is shown in Figure 2.

3.1 Forward propagation of the signal

In a BP neural network, numerous neurons form a hidden layer with a multilayer structure. Each neuron receives input signals from other neurons, which are weighted to obtain a total input value. The neuron compares the total input value with a threshold value, and then the value will be processed by an activation function to obtain the final output [12].

The introduction of the activation function can solve the linear indistinguishability problem and strengthen the expressiveness of the deep neural network [13]. In forward propagation, information enters the network from the input layer and is computed at each layer of the implicit layer in turn to obtain the result of the final output layer. The structure of signal forward propagation is shown in Figure 3.
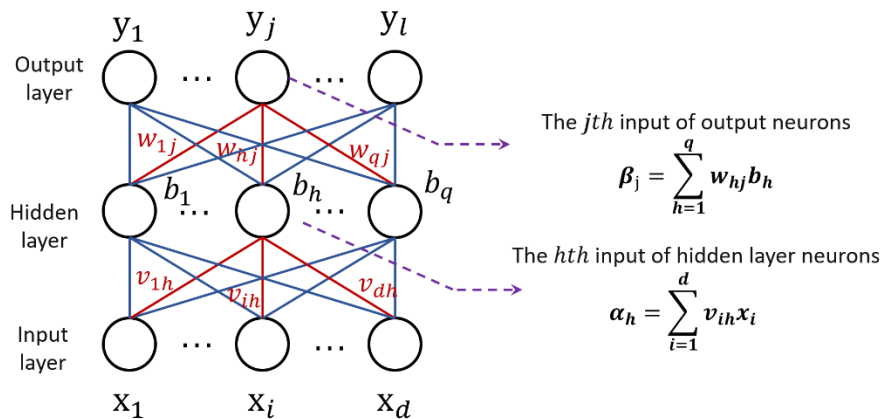

Figure 3: Forward propagation of the signal

We multiply the value of each layer by the corresponding weight and bias variable as the activation function.

From the input layer to the hidden layer, it can be expressed as:

$$\alpha_h = \sum_{i=1}^{d} v_{ih} x_i + \theta_h \tag{7}$$

From the hidden layer to the output layer, it can be expressed as:

$$\beta_j = \sum_{h=1}^{q} w_{hj} b_h + \theta_j \tag{8}$$

Due to the random parameters, there is a large error between the first output and the real result. The back propagation of the model adjusts the parameters according to the error, and as a result, the parameters can be better fitted until the error reaches a minimum value.

3.2 Back propagation of errors

Back propagation makes the error smaller by calculating the error between the output value and the true value, spreading the error among all neurons in each layer, and using the error signal obtained from each layer as the basis for adjusting each parameter.

The formula for calculating the error is as follows:

$$E = \frac{1}{2} \sum_{k=1}^{2} (y_k - T_k)^2 \tag{9}$$

y_k is the output value and T_k is the true value.

The basic idea of BP neural network to reduce the error is using gradient descent method. The neural network uses gradient search to adjust the connection strength and the threshold value of the nodes between the input layer and the hidden layer and the hidden layer and the output layer. As a result, the error decreases along the gradient direction.

The formula for reverse update of weights is as follows:

$$\Delta w_{ij} = (l)Ey_k$$
$$w_{ij} = \Delta w_{ij} + w_{ij}$$

(10)

l is called the learning rate, which can adjust the pace of updating, generally taken as 0.1-0.6.

The steps of BP neural network implementation are as follow.

First, it calculates each neuron input and output. Second, it calculates the partial derivative of the error function with respect to each output layer neuron. Third, it calculates the partial derivative of the error function with respect to the hidden layer neuron. Then, it uses the results of the first two steps to correct the weights, and uses the learning rate to correct the network parameters. The global error is calculated to decide whether the requirements are satisfied. Finally, after several learning trainings, the mean squared error is minimized and the network parameters corresponding to the minimum error are obtained.

At this point, the BP neural network is able to process the input information and output the classification results with minimum error after nonlinear transformation.

4. Experimental results and analysis

4.1 Experimental parameters design

In order to match the simulation with the actual electromagnetic environment, the parameters of the signal simulated in this paper were randomly transformed in the specified range. $U(a, b)$ indicates that the corresponding parameter values are uniformly distributed in the interval from a to b. The sampling frequency $f_s = 65MHz$, f_p, f_1, f_2 indicate the carrier frequency of the signal, τ_{pw} indicates the pulse width of the signal, L indicates the coding length, M indicates the number of codes, and B denotes the bandwidth.

The main parameters of the signal and the characteristic parameters sub-band power ratio are shown in Table 1 and Table 2, respectively.

Table 1: The main parameters of the signal

Signal category	Parameter	Scope
CP	f_p	$U(f_s/6, f_s/4)$
	τ_{pw}	$U(5 \times 10^{-6}, 7.5 \times 10^{-6})$
Costas	f_{min}	$U(f_s/30, f_s/20)$
	t_p	$U(5 \times 10^{-6}, 1 \times 10^{-6})$
	N_c	[2,5]
Frank	f_p	$U(f_s/6, f_s/4)$
	M	[8,10]
BPSK	f_1	$U(f_s/6, f_s/3)$
	f_2	$U(f_s/3, f_s/2)$
	L	$U(15,25)$
	N	$U(16,23)$
LMF	f_p	$U(f_s/6, f_s/4)$
	τ_{pw}	$U(5 \times 10^{-6}, 7.5 \times 10^{-6})$
	B	$U(f_s/20, f_s/10)$

Table 2: Sub-band power ratio of radar signal

Signal category	Sample	G_1	G_2	G_3	G_4	G_5
CP	160	0.9980	0.0012	0.0005	0.0003	0.0002
Costas	160	0.2646	0.3435	0.2525	0.1393	0.1274
Frank	160	0.2935	0.2432	0.2236	0.2398	0.1447
BPSK	160	0.2133	0.2867	0.2842	0.2158	0.0853
LMF	160	0.0207	0.9524	0.0254	0.0015	0.0010

4.2 Experimental results and analysis

We generated simulated signals with 160 samples for each signal, and superimposed Gaussian white noise with a signal-to-noise ratio of 2 dB. 800 total samples were divided into training and test sets according to 7:3, and the classification prediction was performed by BP neural network after feature extraction. The success rate of classification results and the confusion matrix of the test set are shown in Table 3 and Figure 4, respectively.

Table 3: Classification results (2dB)

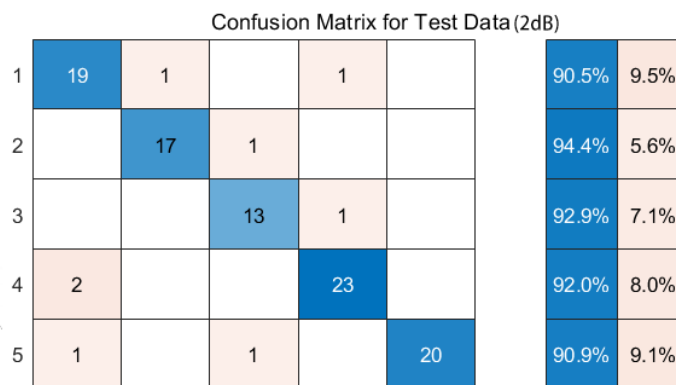| Signal category	Recognition rate/%
CP(y1)	90.5
Costas (y2)	94.4
Frank (y3)	92.9
BPSK (y4)	92.0
LMF (y5)	90.9

Figure 4: Confusion matrix for test data (2dB)

In addition, in order to test the classification system's resistance to interference, 800 samples were also assigned with equal probability between signal-to-noise ratios of -2 ~10 dB in this paper, and the image of the change in the accuracy of the classification system was recorded as shown in Figure 5.
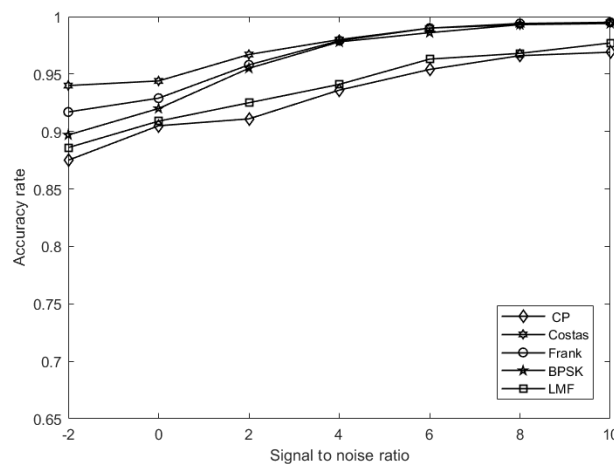

Figure 5: Recognition result of BP neural network

In order to evaluate the classification system's ability, this paper replicated the single-layer neural network studied in the literature [14]. Its main feature is that the affine transformation will be performed before using the activation function in the output layer, which allows it to classify a wider range of classification classes.

In this experiment, we input the same radar signals and overlaid the same Gaussian white noise to the system constructed in the literature [14], and the accuracy of the single-layer neural network in classifying the radar signal was tested at 2 dB intervals between signal-to-noise ratios of 2 ~10 dB. Figure 6 shows the variation lines of classification accuracy between the BP neural network classification method in this paper and the single-layer neural network classification method in the literature [14] (the black line is the BP neural network classification result and the blue line is the single-layer neural network classification result).
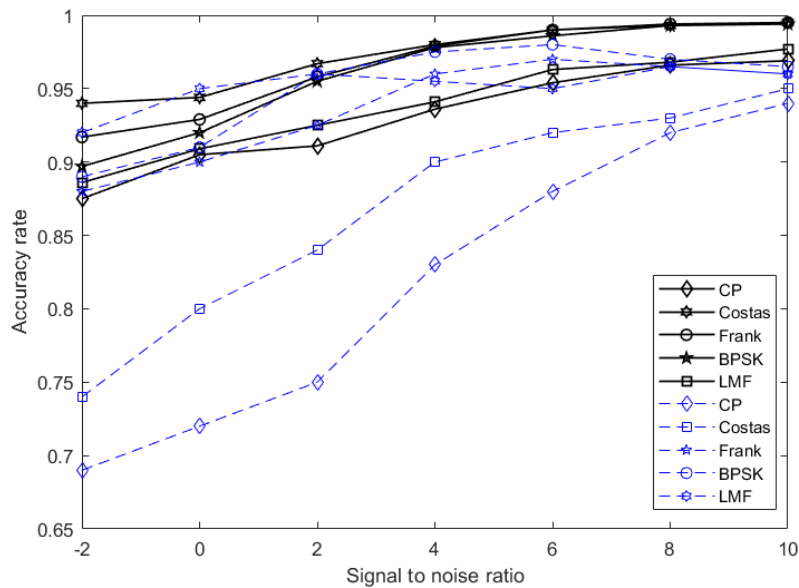

Figure 6: Comparison of results between BP neural network and monolayer neural network

As can be seen from Figure 5 and Figure 6, compared with a single neural network, the classification system in this paper has a higher classification accuracy, especially for radar signals that are not easily distinguishable, and the accuracy is improved by about 10%, effectively reducing the problem of confusing signals with low recognition accuracy. Due to the strong nonlinear mapping ability, adaptive ability and generalization ability of BP neural network, it can accurately solve the complex mechanism inside the signal features and flexibly cope with noise interference. Besides, it also has certain fault tolerance ability to obtain better recognition results.

5. Conclusion

This paper proposes a radar signal classification method based on BP neural network, whose innovation lies in the effective combination of normalized PSD and BP neural network. This method can not only fully extract the information in PSD, but also make use of the powerful nonlinear mapping ability and flexible network structure of BP neural network.

In this paper, we constructed a complex echo signal, extracted features from its PSD, used the sub-band power ratio as the feature parameter, and used the BP neural network as the base learner for training to obtain the final classification results. The simulation experimental results show that the BP neural network can better distinguish different kinds of radar signals compared with the method of individual neural network training.

In the experiments of signal classification and recognition, the recognition rate can still reach more than 85% under the low signal-to-noise ratio, maintaining a good classification accuracy of radar signals. Meanwhile, the classification gap between different radar signals is reduced, with good stability and robustness. In addition, the classification method of this paper has certain superiority compared with similar single-layer neural networks. In summary, the radar signal recognition classification system constructed in this paper has high application value.

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