

Landslide Risk Assessment of Railway Lines Based on Hierarchical Grey Relation Analysis

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Abstract: The risk assessment of landslides is an important component of landslide risk assessment, which is of great significance for the prediction and prevention of landslides. How to scientifically and reasonably select evaluation factors is a weak link in existing research. For the selection of landslide risk assessment factors, the data analysis method mistakenly deleted important factors in factor screening. Therefore, the hierarchical grey relational analysis was first used to calculate the comprehensive correlation degree of the assessment factors based on data analysis and expert experience, and then the random forest model was used to select the best assessment factors and assess the landslide risk. The impact of this method on the model performance was measured by comparing before and after the screening of assessment factors. The results showed that the area under the working characteristic curve of the Random forest model corresponding to the subjects could be increased from 0.82 to 0.91 by screening factors, which improved the prediction accuracy of the evaluation model; Comparing the landslide verification points with higher and high-risk areas, 89.7% of the landslide verification points are consistent with them. The risk assessment of landslides along the railway line based on hierarchical grey correlation analysis selects more reasonable evaluation factors, making the evaluation results more accurate and providing reference basis for risk control of landslides along the Ya'an city railway line.

Keywords: Landslide; Hazard assessment; Hierarchical Grey Relational Analysis; Random forest; Distance function

1. Introduction

The terrain along the West Sichuan Railway in China is steep, with frequent occurrence of moderate to strong earthquakes. The geological environment along the railway is complex, and geological disasters such as landslides, collapses, and mudslides may occur during construction and operation [1]. Landslides pose a serious threat to the lives and property of passengers and railway lines. According to preliminary statistics, there are 126 landslides along the Chengdu Baiyu section of the railway [2]. Landslide danger refers to the possibility of slope sliding and transforming into various forms of disasters under the combined action of multiple influencing factors [3]. The risk assessment of landslides can provide technical support for landslide prevention and control, and the reasonable selection of landslide evaluation factors is an important part of risk assessment.

There have been studies on different methods for selecting factors and evaluating models in landslide risk assessment. Reference [4] used rough set, correlation analysis, and principal component analysis to screen landslide evaluation factors, and used support vector machine models for landslide susceptibility evaluation. Experimental examples showed that screening and reducing evaluation factors can improve the accuracy and accuracy of evaluation results; Literature [5] uses the Apriori algorithm to carry out correlation analysis on landslide evaluation factors and screen factors, and uses the Random forest model to evaluate landslide susceptibility. The experimental results show that the Apriori algorithm is used to select factors from the preselected factors that are more likely to cause landslides, and the evaluation results obtained are more consistent with the actual landslide distribution; Reference [6] used genetic algorithm and rough set to screen landslide evaluation factors, and used BP neural network for landslide susceptibility evaluation, indicating that the reduced factors correspond to higher accuracy of the evaluation model; BP neural network [7], support vector machine [8], Logistic regression [9] and Random forest [10] models have shown good performance in landslide susceptibility assessment; The literature [11] uses Random forest for landslide risk assessment, and compares it with

Logistic regression, Multilayer perceptron and gradient enhancement tree. The results show that the accuracy rate of landslide risk assessment results obtained by Random forest model is the highest. In the above studies, in terms of selecting evaluation factors, some studies have directly selected factors related to landslide events for risk assessment, without considering the contribution of evaluation factors to landslide events, which can easily affect calculation efficiency and accuracy of evaluation results; In terms of evaluation factor screening, the data analysis method is often used to calculate the contribution rate of factors for factor screening. However, there are errors and Outlier in the evaluation factor data extracted from landslide events. When some important factors are eliminated due to data calculation and analysis, the evaluation results will be affected to a certain extent.

To address the issue of mistakenly removing important evaluation factors based on their contribution rate, expert experience and calculation of evaluation factor contribution rate are introduced for factor screening. Firstly, the Analytic Hierarchy Process is used to calculate the subjective weights of the pre-selected factors. Then, grey correlation analysis is used to calculate the correlation degree of the pre-selected factors, and a distance function is introduced to calculate the comprehensive correlation degree of the evaluation factors based on subjective weights and grey correlation degree. Then, the evaluation factors are sorted according to the comprehensive correlation degree from large to small, and the first n factors are used as evaluation factor combinations, which are input into the Random forest model. The final evaluation factor combinations are selected according to the prediction accuracy of the model to complete the screening of evaluation factors, and the importance of evaluation factors is calculated through the Random forest. Finally, ArcGIS is used to stack the factor layers, calculate the landslide risk and generate the landslide risk distribution map in the study area, and complete the landslide risk assessment along the railway.

2. Research methods

2.1 Analytic hierarchy process

The analytic hierarchy process (AHP) is a comprehensive evaluation model method. Through hierarchical and quantitative means, the relevant elements of decision-making problems are divided into multiple levels such as objectives, criteria, and indicators, and a multi-criteria analysis and decision-making method combining qualitative and quantitative analysis [12]. Its use steps are as follows:

- (1) The landslide risk assessment is selected as the target layer, the geological conditions, topographic conditions, and trigger conditions are selected as the criterion layer, and then the initial disaster causing factors are selected as the index layer to build the initial evaluation system;
- (2) The evaluation indexes in the same layer of landslide risk evaluation system are compared and scored, and the judgment matrix is constructed;
- (3) The weight w_1 of each index is obtained by mathematical calculation;
- (4) The consistency index CI and random consistency index CR are introduced to test the consistency of each judgment matrix.

$$CI = \frac{\lambda_{\max} - n}{n - 1} \quad (1)$$

$$CR = \frac{CI}{RI} \quad (2)$$

2.2 Hierarchical grey relational analysis

Landslide is a kind of disaster formed by the influence of many factors, in which the influencing factors are complex and vague, so the occurrence of landslide disaster can be regarded as a grey system. Grey correlation analysis measures the correlation degree between the comparison sample and the reference sample according to the similarity between the indicators [13], to determine the correlation degree of each indicator. The steps of grey correlation analysis are as follows:

- (1) Construct a sample matrix, a total of N groups of samples, each group of samples has a total of M indicators;

(2) Determine the reference sample, which is composed of the optimal value or the worst value of each disaster causing factor;

(3) Due to the different dimensions of a disaster causing factors, the normalized sample matrix is obtained by averaging them;

$$(X_0, X_1, \dots, X_n) = \begin{bmatrix} x_0(1) & x_1(1) & \dots & x_n(1) \\ x_0(2) & x_1(2) & \dots & x_n(2) \\ \vdots & \vdots & \ddots & \vdots \\ x_0(m) & x_1(m) & \dots & x_n(m) \end{bmatrix}$$

(4) Calculate the absolute difference between each comparison sample and the reference sample, that is $|x_0(k) - x_i(k)|, k = 1, 2, \dots, m; i = 1, 2, \dots, n$, secondly calculate the maximum and minimum values of all absolute differences;

(5) Calculate the correlation coefficient;

$$\xi_i(k) = \frac{\min_{i=1}^n \min_{k=1}^m |x_0(k) - x_i(k)| + \rho \max_{i=1}^n \max_{k=1}^m |x_0(k) - x_i(k)|}{|x_0(k) - x_i(k)| + \rho \max_{i=1}^n \max_{k=1}^m |x_0(k) - x_i(k)|} \quad (3)$$

In equation (3) ρ is the resolution coefficient, generally 0.5[14].

(6) The average method is used to calculate the correlation degree;

$$r_i = \frac{1}{m} \sum_{k=1}^m \xi_i(k) \quad (4)$$

(7) The normalized grey correlation degree W_2 is obtained by normalizing the correlation degree;

(8) The distance function[15] is introduced to calculate the comprehensive correlation degree combined with AHP weight and normalized grey correlation degree.

$$L(w_1, w_2) = \sqrt{\frac{1}{2} \sum_{i=1}^m (w_{i1} - w_{i2})^2} \quad (5)$$

Let the comprehensive correlation degree be w and the coefficients of AHP weight and grey correlation degree be a and b respectively, then w is:

$$w = aw_1 + bw_2 \quad (6)$$

Make the difference between grey correlation degree and AHP weight consistent with the difference between distribution coefficients, to eliminate the influence of human factors and data singularity, and obtain relatively objective and accurate results. Therefore, the following constraints are used to calculate the correlation coefficient.

$$\begin{cases} L^2(w_1, w_2) = (a - b)^2 \\ a + b = 1 \end{cases} \quad (7)$$

2.3 Association rules

Association rules are one of the important means of data mining, which mainly refers to finding the correlation of different items in the same event, that is, the correlation between different items in the transaction database [16]. The total set of the chronicle database is X . if subsets A and B of the total set X meet $A \subset X, B \subset X$, and $A \cap B = \emptyset, A \Rightarrow B$ is called association rule, where A and B are the premise and consequence of association rule respectively. Support is the percentage of $A \cup B$ in transaction database x , as shown in equation (8):

$$Support(A \Rightarrow B) = p(A \cup B) \quad (8)$$

Calculate the support degree of landslide caused by each disaster causing factor, and use the support

degree to test the rationality and accuracy of landslide disaster causing factor screening [17].

2.4 Random forest

Random forest (RF) is a combined classifier in machine learning algorithm. N samples ($n < N$) are retrieved from n sample sets, K attributes ($k < K$) are selected from K total attributes, and the best segmentation attributes are selected based on Gini index to create a decision tree. Multiple decision trees can be integrated through bagging algorithm to form a random forest [18]. Random forest training is fast, not easy to "over fit", and has a good tolerance for noise and outliers [19]. The importance of RF is calculated based on *gini* index. The calculation formula of *gini* index is as follows:

$$gini(A) = 1 - \sum_{i=1}^n p_i^2 \quad (9)$$

$$gini(A, B) = \sum_{j=1}^m \frac{|A_j|}{|A|} gini(A_j) \quad (10)$$

In formula (9), n is the number of classification categories in sample A (whether landslide disaster occurs); p_i is the proportion of class i samples in sample A. In equation (10), $gini(A, B)$ is the *gini* index after dividing sample A by factor B ; m is the total number of samples; $|A_j|$ is the number of j samples. After averaging the importance results output from each decision tree, it is the importance of the random forest.

3. Landslide risk assessment model

The flow chart of landslide risk assessment is shown in Figure 1.

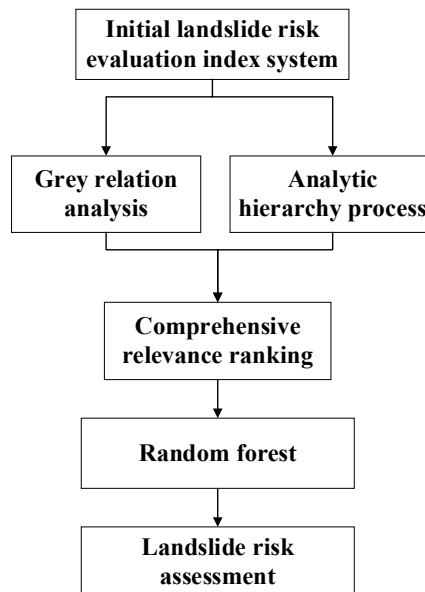


Figure 1: Flow chart of landslide risk assessment

(1) Firstly, score the initial evaluation index system and construct the judgment matrix, so as to calculate the subjective weight of each factor and test the consistency of the judgment matrix. At the same time, the grey correlation method is used to analyze the initial indexes and calculate the grey correlation degree of each factor. The comprehensive correlation degree is calculated by using the distance function,

(2) The factors are sorted according to the comprehensive correlation degree from large to small. Take the first n factors and input them into the random forest model. Select the corresponding factor combination with the highest accuracy, eliminate the factors that do not appear in the factor combination, and complete the factor screening. Then the association rules are used to calculate the

support of each factor to verify the rationality and accuracy of factor screening.

(3) After the factor screening, use the random forest to calculate the importance of each factor, set and optimize multiple parameters in the random forest, improve the classification accuracy of the model, and obtain the importance of each factor. Use ArcGIS to assign values and overlay analysis to each factor layer, calculate the landslide risk size and generate the landslide risk distribution map, and complete the landslide in Ya'an-Batang section of Sichuan-Tibet railway Risk assessment.

4. Research area and data source

4.1 Overview of the study area

Figure 2 is the railway route map of Ya'an City. Ya'an City is complex and changeable, the fault structure is developed, the geological disasters are many and wide, the dangerous situation is serious and the harm is great, and the rainfall frequency is intensive from June to August every year. The rainfall is mostly heavy rain and heavy rainstorm, and the landslide types are mostly rainfall type landslide and earthquake type landslide. The triggering conditions of landslide disaster in this study only consider rainfall and human engineering activities, not the earthquake.



Figure 2: Study area

4.2 Data sources

Based on the existing research[20,21], 12 disaster causing factors are selected, namely rainfall, formation lithology, distance to fault, land use type, slope, elevation, slope direction, plane curvature, profile curvature, distance to river, vegetation coverage and human engineering activities. These factors can comprehensively present the geological conditions, topographic conditions, and triggering conditions of landslide disasters in the study area.

The data sources are as follows: the rainfall data is from the China Meteorological data network. The maximum 24h rainfall in the current rainfall process is selected to represent the rainfall factor; The data of formation lithology and distance to fault are from the national geological data center; Land use types and landslide disaster distribution are derived from the resource and environmental science and data center; The distance to the river is derived from the basic geographic information database; Human engineering activities are represented by road buffer zone and residential area, and the road buffer zone originates from OSM(<https://www.openstreetmap.org/>), the residential area originates from network collection; Landsat8 and DEM data are derived from geospatial data cloud, vegetation coverage is extracted from landsat8, and slope, aspect, plane curvature, and section curvature are extracted from DEM.

5. Example analysis and discussion

5.1 Subjective weight calculation based on AHP

The initial landslide risk evaluation index system is constructed according to 12 initial hazard factors, as shown in Figure 3. The evaluation indexes are scored, the judgment matrix A is constructed based on the geological conditions, topographic conditions and trigger conditions in Figure 3, and the judgment matrices B_1 , B_2 and B_3 are constructed based on the hazard factors under geological conditions, topographic conditions and trigger conditions.

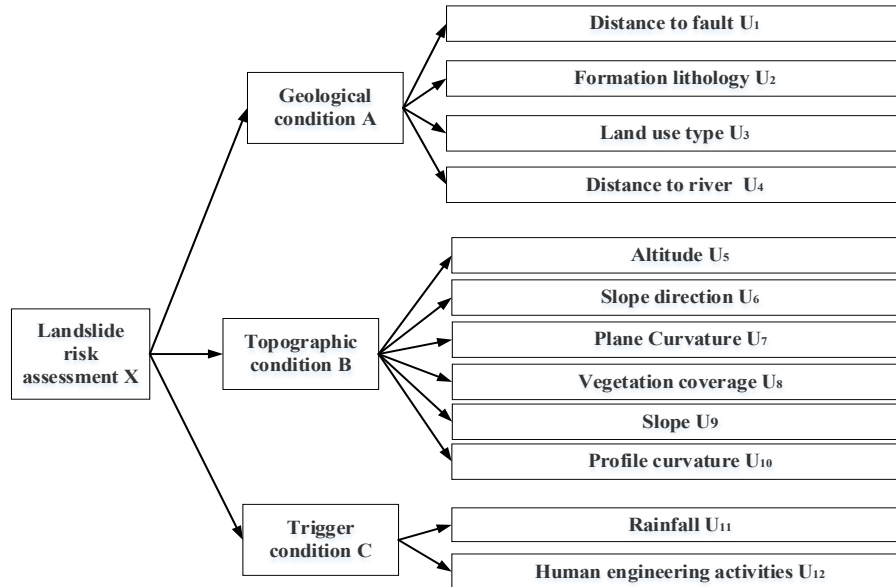


Figure 3: Initial landslide risk evaluation index system

$$A = \begin{bmatrix} 1 & 3 & 2 \\ 4 & 4 & 3 \\ 3 & 1 & 4 \\ 3 & 4 & 1 \\ 2 & 5 & 1 \end{bmatrix} \quad
 B_1 = \begin{bmatrix} 1 & 4 & 4 & 2 \\ 5 & 5 & 3 & 3 \\ 4 & 1 & 5 & 2 \\ 3 & 3 & 1 & 6 \\ 4 & 5 & 1 & 5 \\ 3 & 1 & 5 & 1 \\ 2 & 2 & 6 & 1 \end{bmatrix} \quad
 B_2 = \begin{bmatrix} 1 & 6 & 3 & 4 & 4 & 4 \\ 5 & 5 & 2 & 3 & 5 & 3 \\ 6 & 1 & 11 & 9 & 3 & 4 \\ 2 & 10 & 10 & 10 & 4 & 3 \\ 3 & 11 & 1 & 4 & 2 & 9 \\ 3 & 10 & 5 & 5 & 5 & 10 \\ 4 & 9 & 4 & 1 & 2 & 6 \\ 5 & 4 & 5 & 3 & 1 & 2 \\ 4 & 3 & 2 & 2 & 1 & 2 \\ 5 & 3 & 10 & 5 & 1 & 1 \\ 7 & 4 & 9 & 6 & 2 & 1 \end{bmatrix} \quad
 B_3 = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$$

The eigenvectors of each judgment matrix are calculated, and the eigenvectors of each disaster causing factor are obtained importance w_1 , check the consistency of each judgment matrix through equations (1) and (2), as shown in Table 1.

$$w_1 = (0.062, 0.081, 0.064, 0.054, 0.057, 0.055, 0.049, 0.058, 0.87, 0.052, 0.253, 0.127)$$

Table 1: Consistency test results of each judgment matrix

| | A | B1 | B2 | B3 |
|-----------|--------|--------|--------|----|
| λ | 3.0015 | 4.0471 | 6.0300 | 2 |
| CI | 0.0007 | 0.0157 | 0.0060 | 0 |
| CR | 0.0015 | 0.0176 | 0.0047 | 0 |

5.2 Calculation of correlation degree of disaster causing factors based on grey relation

12 preselected factors such as fault distance and formation lithology are selected as the indexes of

grey correlation analysis. The extracted initial landslide data are processed by the mean method, and the reference samples are determined:

$$X_0=(1.6,2,1.02,1.33,1.42,1.6,2.3,1.2,1.1,1.2,1.42,1.17)$$

Calculate the absolute difference between the comparison sample and the reference sample, and determine the maximum and minimum values of the absolute difference. The correlation degree is calculated according to equations (3) and (4):

$$r=(0.872,0.548,0.499,0.476,0.831,0.85,0.502,0.899,0.923,0.542,0.893,0.881)$$

The grey relation degree is normalized to:

$$r_1=(0.1,0.063,0.057,0.055,0.095,0.098,0.058,0.103,0.106,0.062,0.102,0.1)$$

The comprehensive relation degree obtained from equation (5) is:

$$Z=(0.081,0.071,0.06,0.054,0.076,0.076,0.053,0.08,0.096,0.055,0.177,0.11)$$

5.3 factor screening and inspection

Rank the factors in the comprehensive correlation degree z from large to small, Take the first n factors as data sets and input them into the random forest model ($n = 5, 6, \dots, 12$). ROC curve is called sensitivity curve, which has been widely used in the accuracy analysis of geological hazard risk assessment results[22]. AUC represents the area under the ROC curve. The closer the AUC value is to 1, it shows that the discrimination result of the model is better. As shown in Figure 4, after inputting the random forest model through different factor combinations, the ROC curve is generated and the AUC value is calculated. When $n = 8$, the corresponding model accuracy is the largest, and the AUC value is 0.89. Therefore, keep these 8 factors, eliminate the distance to fault, distance to the river, plane curvature, and section curvature, and complete the factor screening. The association rule formula (8) is used to calculate the support of the above-retained factors, and the obtained support is 0.94, 0.941, 0.824, 0.912, 0.81, 0.891, 0.906, and 0.912, which are greater than 0.8. Therefore, this method is reasonable for screening landslide risk assessment indicators.

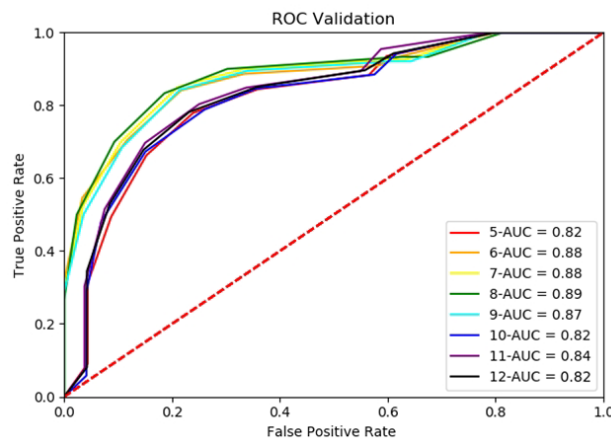


Figure 4: Test results of random forest ROC curve of eight factor combinations

Python is used to calculate the importance of each factor in the random forest model. Firstly, the size of each parameter is set, and then the parameters are adjusted. The optimal values of each parameter are obtained by grid search and 10 fold cross verification. Finally, the importance w_2 of the eight factors of rainfall, human engineering activities, slope, stratum lithology, vegetation coverage, slope direction, elevation, and land use type is obtained through *feature_importances* function.

$$w_2=(0.201,0.17,0.154,0.141,0.102,0.096,0.072,0.063)$$

5.4 landslide risk assessment in the study area

On the basis of each factor layer, the important weight is given to each layer by using the spatial superposition function of ArcGIS, and the landslide risk distribution map of the study area is generated, as shown in Figure 5. Based on the natural breakpoint method, the landslide risk evaluation results are divided into five levels: low, low, medium, high and high risk. It is generally believed that the high-risk

and high-risk areas are vulnerable to landslides. When 97 landslide verification points are used to test the landslide risk assessment results, it can be obtained that 89.7% of the landslide points are located in the high-risk and high-risk areas, that is, it is considered that the verification accuracy is 89.7%. According to the statistical analysis of the risk assessment results in Figure 5, the railway lines in high and high-risk areas are 10.9 km (2.1%) and 48.7 km (9.4%) respectively and are mostly distributed in Ya'an area. The main reason is that Ya'an has large rainfall, which is easy to reduce the shear strength of the slope and accelerate the disintegration and destruction of the slope. Among them, the maximum 24h rainfall in August 2020 is 425.2mm, Reaching an all-time high. At the same time, human engineering activities in this area are strong, roads and residential areas are densely distributed, which provides a good disaster pregnant environment for the landslide. For the above high-risk lines, it is recommended to use scientific means to monitor the dangerous slopes during line construction, and take preventive measures against landslides in advance, so as to prevent landslides from causing huge damage to the railway line. During the later operation of Sichuan-Tibet railway, the landslide hazard assessment results are closely combined with the railway signal early warning system to ensure the safe operation of trains and the safety of lines, and provide a safety guarantee for railway operation.

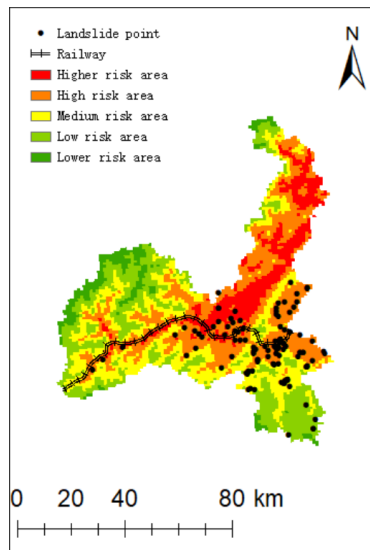
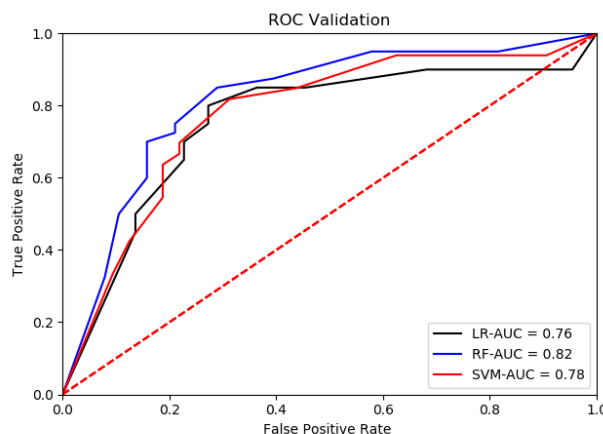


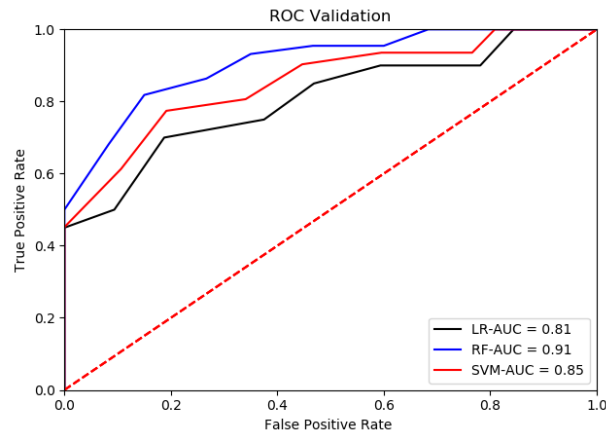
Figure 5: Landslide risk zoning map of the study area

5.5 Accuracy verification of different models

The random forest model is combined with the support vector machine (SVM) model and logistic regression model commonly used in landslide risk assessment (LR) to compare the model accuracy before and after screening factors. As shown in Figure 6, the accuracy of random forest model before screening factors is the largest, and its AUC area is 0.82. After comprehensive correlation screening factors and random forest parameter optimization, the AUC area of random forest model is increased to 0.91, which is greater than 0.81 of logistic regression and 0.85 of support vector machine.



(a) Test results of ROC curve of each model without screening factor



(b) ROC curve test results of each model after screening factors

Figure 6: ROC curve verification

6. Conclusion

Based on the grey correlation and AHP screening factors, the random forest model is used to evaluate the landslide risk. Taking Ya'an city railway lines as the research object, the following conclusions are obtained:

(1) The grey relation and analytic hierarchy process are used to comprehensively screen the factors, which solves the problem of false deletion of factors due to a small grey correlation degree. The results show that rainfall, slope, human engineering activities, formation lithology, vegetation coverage, slope direction, elevation, and land use type are strongly related to the occurrence of landslide disaster in Ya'an city railway lines.

(2) The random forest model is used to evaluate the landslide risk, and the ROC curve is used to evaluate the accuracy of the random forest model. The area under the ROC curve before the screening factor is 0.82, and the area under the ROC curve after the optimization of the screening factor and random forest parameters is 0.91. It is proved that the optimization of the screening factor and model parameters can improve the accuracy of the evaluation model.

(3) The landslide risk assessment results obtained based on the research method in this paper are consistent with the landslide disaster verification points in Sichuan Province, which proves that the research method in this paper is reliable, accurate and has certain practical value. It can provide some result reference and technical support for the medium-term construction and later operation management of Ya'an Railway.

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